On internal validity in multiple baseline designs

James E. Pustejovsky The University of Texas at Austin pusto@austin.utexas.edu

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# Single-case designs

- Core features:
  - Repeated measurements on a small number of individual cases.
  - Within-case comparisons of outcomes under different treatment conditions.
- Growing interest in statistical analysis, effect size measures, meta-analytic methods for single-case studies.
- Multiple baseline is most common single-case design (Shadish & Sullivan, 2011)

#### Sigurdsson & Austin (2008). Using real-time visual feedback to improve posture at computer workstations



# Multiple baseline design (MBD)

- Key features for internal validity:
  - Deliberate introduction of treatment to cases
  - Staggered treatment introduction across cases
- My argument:
  - Appropriate analytic method depends on the specific treatment assignment mechanism.
  - Statistical analysis should account for staggered treatment introduction to maintain internal validity.

## Notation and model

Structural model:

$$Y_{ij}(T_i) = \beta_{0i} + \beta_{1i} X_{ij}(T_i) + e_{ij}$$
  

$$\beta_{0i} = \gamma_0 + u_{0i}$$
  

$$\beta_{1i} = \gamma_1 + u_{1i}$$
 Average treatment effect

- *m* cases
- *n* measurement occasions
- *Y<sub>ij</sub>* outcome for case *i* at time *j*, i = 1,...,*m*, j = 1,...,*n*
- $T_i$  length of baseline phase for case *i*
- $X_{ij} = 0$  if case *i* is in baseline at time  $j (j \le T_i)$
- $X_{ij} = 1$  if case *i* is in treatment at time *j* (*j* >  $T_i$ )

## Random assignment of treatment times

- Uncommon in practice.
- Understood to improve internal validity (Kratochwill & Levin, 2010)
- Analytic model 1 (cf. Van den Noortgate & Onghena, 2003):

$$\begin{pmatrix} Y_{ij} \mid X_{i1}, \dots, X_{in} \end{pmatrix} = \beta_{0i} + \beta_{1i} X_{ij} + e_{ij}$$
$$\beta_{0i} = \gamma_0 + u_{0i}$$
$$\beta_{1i} = \gamma_1 + u_{1i}$$

## Triage on known baseline ranks

- Suppose that...
  - Fixed set of baseline lengths  $t_1, t_2, ..., t_m$ .
  - Baseline lengths are assigned prior to start of study.
  - Investigator can accurately predict baseline outcome levels  $\beta_{01}$ ,  $\beta_{02}$ ,...,  $\beta_{0m}$ .
- Triage on known baseline ranks:
  - Case with lowest baseline starts treatment first.
  - Case with 2<sup>nd</sup> lowest baseline starts treatment second.
  - Etc.

## Triage on known baseline ranks

• Treatment effect estimator from Analytic Model 1 has negative bias.



#### Triage on known baseline ranks

• Centering the treatment indicator by case mitigates the bias.



## Triage on measured baseline ranks

- Triage based on running mean outcomes as of each possible treatment assignment time.
- Case with lowest measured baseline as of time  $t_1$  receives treatment first.
- Of the remaining cases, case with lowest measured baseline as of time  $t_2$  receives treatment second.
- Etc.

#### Triage on measured baseline ranks

• Treatment effect estimator based on Analytic Model 1 has negligible biases.



#### Triage on measured baseline ranks

• Treatment effect estimator based on Analytic Model 2 has larger, positive biases.



# Implications

- Empirical researchers using MBDs should explain how they assign treatment times to cases.
- Methodologists should specify treatment assignment mechanisms for which a proposed analytic method is valid.
- Other assignment mechanisms used in practice?